A Software for Complete Calibration of Multicamera Systems

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Outline



- Problem definition
- Proposed solution
- Results
- Applications



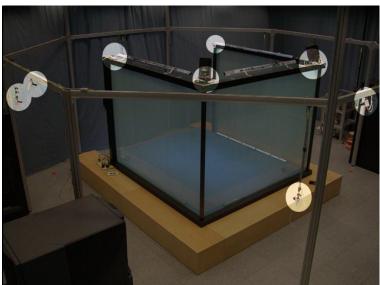
Motivation

- multiple cameras became common
- they can be found in . . .









Telepresence setup





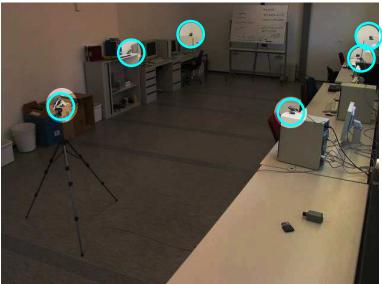
Calibration



- many tasks can be accomplished without knowing anything about the cameras
- however, many more when we know . . .

camera positions, and . . .

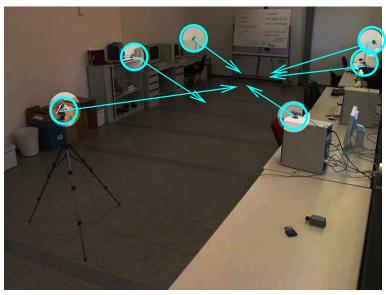


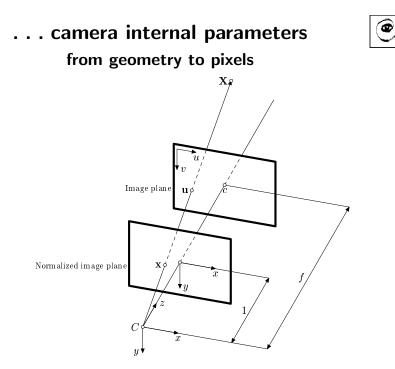


... camera orientations, and ...



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. . . nonlinear parameters included





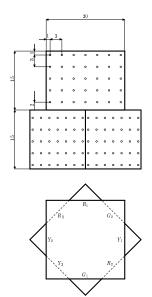
Camera calibration is an old problem



- for photogrammetrists (even older problem)
- in computer vision
- many methods exist

Classical approaches — known 3D points

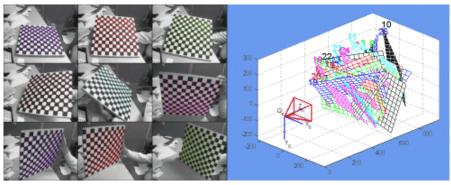






Classical approaches — plate at several positions





http://www.vision.caltech.edu/bouguetj/calib_doc/

Classical methods — revisited



Pros:

- many methods (and free codes)
- precise, even for complicated camera models

Cons (for multicamera systems):

- lacksim many cameras ightarrow hand work is not an option
- ♦ large working volume to fill → big calibration objects/plates

Our solution — overview

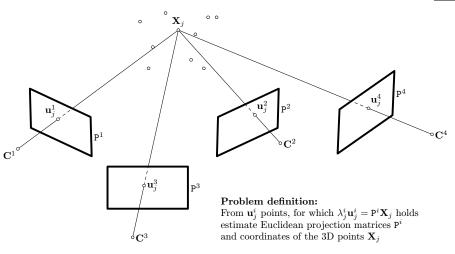


We assume at least approximately synchronized multicamera $(N \ge 3)$ setup.

- use 1-point calibration object easily detectable in images
- wave the calibration point through the working volume freely
- this will create a virtual calibration object (but the 3D position unknown!)
- apply theoretical results from self-calibration field
- estimate as complicated camera model as reasonable
- validate the results

Multiple cameras — Geometry



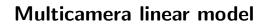


Pinhole camera model

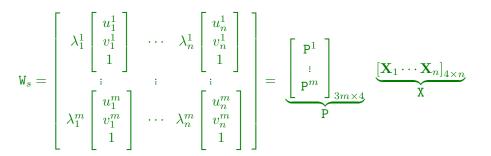


$$\lambda_j^i \left[egin{array}{c} u_j^i \ v_j^i \ 1 \end{array}
ight] = \lambda_j^i \mathbf{u}_j^i = \mathtt{P}^i \mathbf{X}_j \,, \qquad \lambda_j^i \in \mathcal{R}^{-1}$$

- $ullet_{j}$ index points
- igstarrow i index camera
- λ_{i}^{i} projective depths
- \mathbf{u}_{i}^{i} point projections (we find them in images)
- \mathbf{X}_j 3D points (we do not know the positions!)
- Pⁱ camera matrices







Self-calibration (Euclidean stratification)

$$\mathbf{W}_s = \mathbf{P}\mathbf{X} = \mathbf{P}\mathbf{H} \mathbf{H}^{-1}\mathbf{X} = \hat{\mathbf{P}}\hat{\mathbf{X}},$$

What the software does:



- 1. Finds the projections \mathbf{u}_{i}^{i} of the laser pointer in the images.
- 2. Discards misdetected points by pairwise RANSAC analysis.
- 3. Estimates projective depths λ_j^i and fills the missing points to make scaled measurement matrix W_s complete.
- 4. Performs the rank 4 factorization of the matrix W_s to get projective shape and motion and upgrades them to Euclidean ones.
- 5. Estimates the parameters of the non-linear distortion
- 6. Optionally, if some true 3D information is known, aligns the computed Euclidean structures with a world system.

Many cross-validation steps inside.

Calibration object





A very standard laser pointer with a piece of transparent plastic attached.

Finding points



Needs to be a bit more clever than a simple thresholding

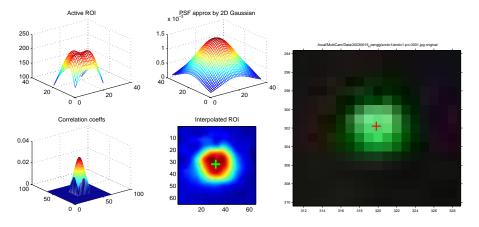


Statistical analysis of the images (almost) solves it.

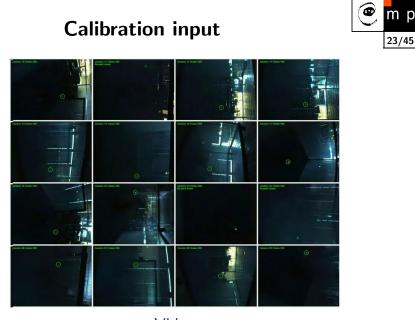
Finding points



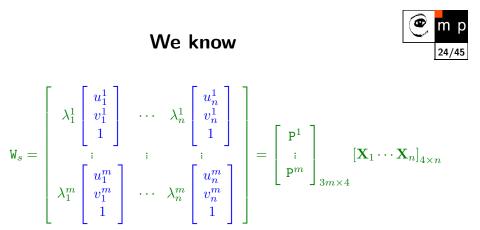
Sub-pixel accuracy is desirable



Around 100 ms per image.







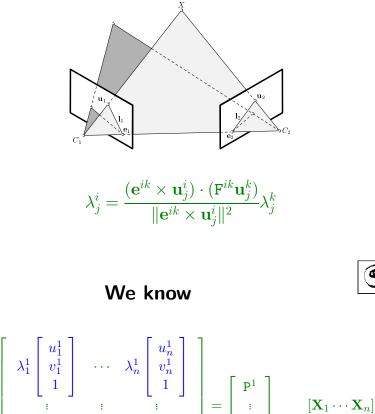
 $\mathbf{W}_s = \mathbf{P}\mathbf{X} = \mathbf{P}\mathbf{H}\mathbf{H}^{-1}\mathbf{X} = \hat{\mathbf{P}}\hat{\mathbf{X}},$

However, some $[u^i_j,v^i_j]^\top$ may be missing!





uses the epipolar geometry

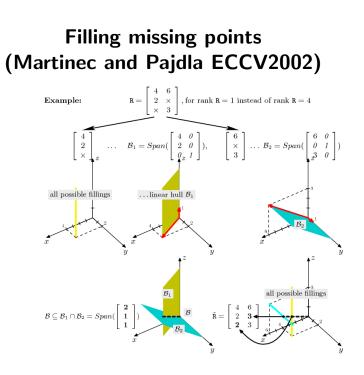




$$\mathbb{W}_{s} = \begin{bmatrix} \lambda_{1}^{1} \begin{bmatrix} u_{1}^{1} \\ v_{1}^{1} \\ 1 \end{bmatrix} & \cdots & \lambda_{n}^{1} \begin{bmatrix} u_{n}^{1} \\ v_{n}^{1} \\ 1 \end{bmatrix} \\ \vdots & \vdots & \vdots \\ \lambda_{1}^{m} \begin{bmatrix} u_{1}^{m} \\ v_{1}^{m} \\ 1 \end{bmatrix} & \cdots & \lambda_{n}^{m} \begin{bmatrix} u_{n}^{m} \\ v_{n}^{m} \\ 1 \end{bmatrix} \end{bmatrix} = \begin{bmatrix} \mathbb{P}^{1} \\ \vdots \\ \mathbb{P}^{m} \end{bmatrix}_{3m \times 4} [\mathbf{X}_{1} \cdots \mathbf{X}_{n}]_{4 \times n}$$

 $\mathbf{W}_s = \mathbf{P}\mathbf{X} = \mathbf{P}\mathbf{H}\mathbf{H}^{-1}\mathbf{X} = \hat{\mathbf{P}}\hat{\mathbf{X}} \ ,$

However, some $[u^i_j,v^i_j]^{\top}$ and λ^i_j may be missing!





We know



$$\mathbf{W}_{s} = \begin{bmatrix} \lambda_{1}^{1} \begin{bmatrix} u_{1}^{1} \\ v_{1}^{1} \\ 1 \end{bmatrix} & \cdots & \lambda_{n}^{1} \begin{bmatrix} u_{n}^{1} \\ v_{n}^{1} \\ 1 \end{bmatrix} \\ \vdots & \vdots & \vdots \\ \lambda_{1}^{m} \begin{bmatrix} u_{1}^{m} \\ v_{1}^{m} \\ 1 \end{bmatrix} & \cdots & \lambda_{n}^{m} \begin{bmatrix} u_{n}^{m} \\ v_{n}^{m} \\ 1 \end{bmatrix} \end{bmatrix} = \begin{bmatrix} \mathbf{P}^{1} \\ \vdots \\ \mathbf{P}^{m} \end{bmatrix}_{3m \times 4} [\mathbf{X}_{1} \cdots \mathbf{X}_{n}]_{4 \times n}$$

$$\mathbf{W}_s = \mathbf{P}\mathbf{X} = \mathbf{P}\mathbf{H}\mathbf{H}^{-1}\mathbf{X} = \hat{\mathbf{P}}\hat{\mathbf{X}} \ ,$$

Rank-4 factorization



$$\mathbf{W}_{s} = \begin{bmatrix} \mathbf{P}^{1} \\ \vdots \\ \mathbf{P}^{m} \end{bmatrix}_{3m \times \mathbf{4}} [\mathbf{X}_{1} \cdots \mathbf{X}_{n}]_{\mathbf{4} \times n}$$

So, matrix \mathbb{W}_{s} should have rank at most 4

$$\begin{split} \mathbf{W}_{s} &= \mathbf{U} \mathbf{S} \mathbf{V}^{\top} \\ \begin{bmatrix} \mathbf{P}^{1} \\ \vdots \\ \mathbf{P}^{m} \end{bmatrix}_{3m \times 4} [\mathbf{X}_{1} \cdots \mathbf{X}_{n}]_{4 \times n} = (\mathbf{U} \sqrt{\mathbf{S}_{4}})(\sqrt{\mathbf{S}_{4}} \mathbf{V}^{\top}) \end{split}$$

where ${\tt S}_4$ is the ${\tt S}$ with only 4 biggest diagonal values, rest is zeroed.





 $\mathbf{W}_s = \mathbf{P}\mathbf{X} = \mathbf{P}\mathbf{H}\mathbf{H}^{-1}\mathbf{X} = \hat{\mathbf{P}}\hat{\mathbf{X}} \ ,$

We must find a 4×4 matrix H which upgrades the projective structures P, X to metric ones, $\hat{P}, \hat{X}.$

Euclidean stratification (Pollefeys et al, Hartley, ...)



based on the idea of absolute quadric (conic)

$$\hat{\mathbf{P}}^i = \mu_i \left[egin{array}{cc} \mathbf{K}^i \mathbf{R}^i & \mathbf{K}^i \mathbf{t}^i \end{array}
ight]$$

$$\hat{\mathbf{P}}^{i}\hat{\Omega}_{\infty}\hat{\mathbf{P}}^{i op}\sim\mathbf{K}^{i}\mathbf{K}^{i op}$$

where

$$\hat{\Omega}_{\infty} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

Euclidean stratification cont.



absolute conic exists also in the projective world!

$$\begin{array}{lll} \mathsf{K}^{i}\mathsf{K}^{i\top} & \sim & (\hat{\mathsf{P}}^{i}\mathsf{H}^{-1})(\mathsf{H}\hat{\Omega}_{\infty}\mathsf{H}^{\top})(\mathsf{H}^{-\top}\hat{\mathsf{P}}^{i\top}) \\ \mathsf{K}^{i}\mathsf{K}^{i\top} & \sim & \mathsf{P}^{i}\Omega_{\infty}\mathsf{P}^{i\top} \end{array}$$

We know the projective ${\bf P}^i.$ The projective Ω_∞ is 4×4 symmetric.

Once Ω_∞ is known, then we can compute ${\tt H}$ from

$$\boldsymbol{\Omega}_{\infty} = \mathbf{H} \hat{\boldsymbol{\Omega}}_{\infty} \mathbf{H}^{\top}$$

by eigenvalue decomposition and get the sought Euclidean structures $\hat{P}^i = P^i H$ and $\hat{\mathbf{X}}_j = H^{-1} \mathbf{X}_j$.

Euclidean stratification — Example of solution



assume everything is known except focal lenghts

$$\mathbf{K}^{i} = \left[\begin{array}{ccc} f^{i} & 0 & u^{i}_{0} \\ 0 & \alpha^{i} f^{i} & v^{i}_{0} \\ 0 & 0 & 1 \end{array} \right] \rightarrow \mathbf{K}^{i} \mathbf{K}^{i\top} = \left[\begin{array}{ccc} f^{i2} & 0 & 0 \\ 0 & f^{i2} & 0 \\ 0 & 0 & 1 \end{array} \right]$$

Remember that $\mathbf{K}^{i}\mathbf{K}^{i\top}\sim\mathbf{P}^{i}\boldsymbol{\Omega}_{\infty}\mathbf{P}^{i\top}$

$$\begin{split} (\mathbf{P}^{i}\Omega_{\infty}\mathbf{P}^{i\top})_{11} - (\mathbf{P}^{i}\Omega_{\infty}\mathbf{P}^{i\top})_{22} &= 0\\ (\mathbf{P}^{i}\Omega_{\infty}\mathbf{P}^{i\top})_{12} &= 0\\ (\mathbf{P}^{i}\Omega_{\infty}\mathbf{P}^{i\top})_{13} &= 0\\ (\mathbf{P}^{i}\Omega_{\infty}\mathbf{P}^{i\top})_{23} &= 0 \end{split}$$

Each camera contributes by 4 contraints.

We have the metric linear model



$$\mathbf{W}_s = \hat{\mathbf{P}}\hat{\mathbf{X}}$$

Estimation of non-linear distortion starts from

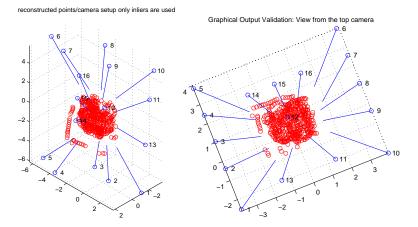
 $\hat{\mathtt{X}}_{j} \leftrightarrow \mathbf{u}_{j}^{i}$

correspondences. We use the CalTech package http://www.vision.caltech.edu/bouguetj/calib_doc/

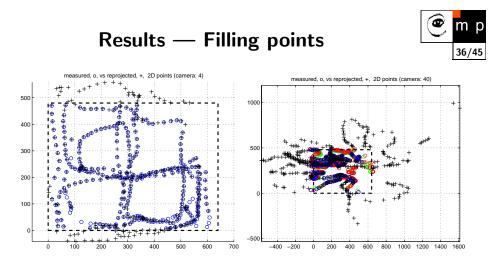
Then it goes back, adapt parameters and . . .







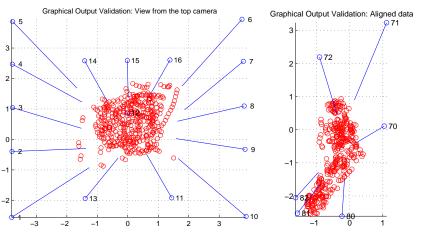
User provides some 3D information. Example: "Cameras No. 11,13,15 define the xy plane".

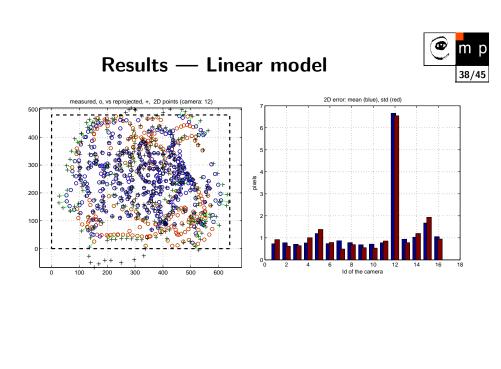


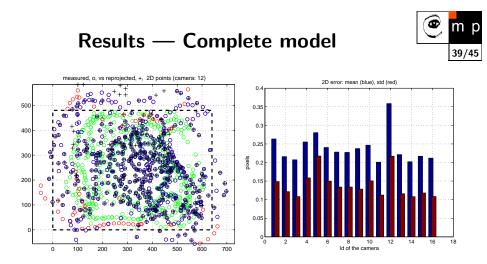
The calibration "point" needs not to be visible in all cameras!

Results — Calibrated setups









Very fine results from (almost) nothing!

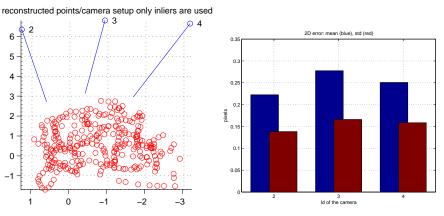


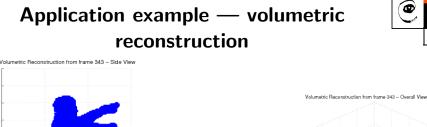


0

m p

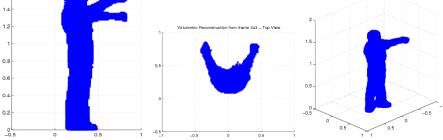
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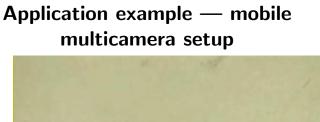


1.8

1.6



I know, it is just toy example. Still, it shows that the metric is OK.







Video

Mobile multicamera setup - worker 3D tracking

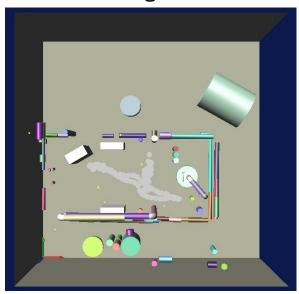




Video

Mobile multicamera setup - worker 3D tracking







Summary

- waving the point object is the only hand work required
- no user interaction
- complete calibration of 16 camera setup may be done in 60-90 minutes (95% computation)

Codes, sample data, papers, etc. downloadable from http://cmp.felk.cvut.cz/~svoboda/SelfCal