# **FACE RECOGNITION:** ROBUSTTRANSFER LEARNING USING THE **MULTIVERSE LOSS**

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🕐 🚾 P The 38th Pattern Recognition and Computer Vision Colloquium, March 2016

#### ACK: I will present work done in collaboration with

TAU students:

#### Etai Littwin, Dedi Gadot, Tomer Galanti

FAIR researchers:

Yaniv Taigman, Ming Yang, Marc'Aurelio Ronzato

### Why faces?

- The most frequent entity in the media by far: e.g. ~1.2 faces / Photo on avg
- 2. Understanding identification
- One class, billions of instances



#### **Challenges in Unconstrained Face Recognition**

1. Pose

2. Illumination

3. Expression

4. Aging

Probes for example

5. Occlusion

























#### 13,233 photos of 5,749 celebrities



Labeled faces in the wild: A database for studying face recognition in unconstrained environments, Huang, Jain, Learned-Miller, ECCVW, 2008

#### **Face verification**





!=





#### Progress over the past 7 years

Accuracy / year

Reduction of error wrt human / year



Labeled Faces in the Wild: A Database for Studying Face Recognition in Unconstrained Environments (results page), Gary B. Huang, Manu Ramesh, Tamara Berg and Erik Learned-Miller.

#### **Face Recognition Pipeline**



#### Deep Neural Networks on aligned inputs



Localization	Front-End ConvNet	Local (Untied) ConvNet	Globally Connected
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Taigman, Yang, Ranzato, Wolf. DeepFace: Closing the Gap to Human-Level Performance in Face Verification. CVPR, 2014.

#### Deep Neural Networks on aligned inputs

Transfer Learning

Connected

ConvNet



Taigman, Yang, Ranzato, Wolf. DeepFace: Closing the Gap to Human-Level Performance in Face Verification. CVPR, 2014.

#### SFCTraining Dataset



4.4 million photos blindlysampled, belonging to morethan 4,000 identities

#### SFC Training Dataset



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Many images per person, but not too many identities

Q1: What is better for learning a *generic* face representation: more identities or more samples per identity?

Galanti, Wolf, Hazan. A Theoretical Framework for Deep Transfer Learning. IMAIAI, 2016

#### The tradeoffs that govern transfer learning

- For a given budget of samples. How to split between classes and samples per class.
- II. Having too many samples and not enough classes leads to overfitting. But not the other way around.
- III. The size of the representation and the number of training samples.
- IV. Saturation.

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### What size representation is ideal?

The network <u>overfits less</u> on the <u>SOURCE</u> training set, and performs better on the <u>TARGET</u> when reducing the representation layer (F7) from 4K dims to 256 dims.





## Can the data suggest optimal dim?

- The dimensionality of the representations is mostly wasted
  - Full rank representation
  - Decisions made based on few dims





Multiverse: 35D, good separation



Littwin, Wolf. The Multiverse Loss for Robust Transfer Learning. CVPR 2016

## Our goals

- Reduce the dimensionality of the representation
- Improve the disciminative power of each dimension
- Let the data speak
   No extra parameter



### A conventional network



 $F \in \mathbb{R}^{d \times c}$ where c is #classes d is the representation dim

### A conventional network

 $\sum_{i=1}^{n} -\log \frac{e^{d_i^{\mathsf{T}} f_{y_i} + b_{y_i}}}{\sum_{j=1}^{c} e^{d_i^{\mathsf{T}} f_j + b_j}}$ 



 $F \in \mathbb{R}^{d \times c}$ where c is #classes d is the representation dim



 $F^i \in \mathbb{R}^{d \times c}$ where c is #classes d is the representation dim



 $F^i \in \mathbb{R}^{d \times c}$ where c is #classes d is the representation dim



 $F^i \in \mathbb{R}^{d \times c}$ where c is #classes d is the representation dim

## **Enforcing orthogonality**

Enforce orthogonal solutions:

$$\begin{split} F^1 &= [f_1^1, f_2^1, \dots, f_c^1] \\ F^2 &= [f_1^2, f_2^2, \dots, f_c^2] \end{split} \quad \forall_j f_j^1 \bot f_j^2 \end{split}$$

Practically, the loss used is:

$$L' = \sum_{i=1}^{n} -\log \frac{e^{d_i^{\mathsf{T}} f_{y_i}^1 + b_{y_i}^1}}{\sum_{j=1}^{c} e^{d_i^{\mathsf{T}} f_j^1 + b_j^1}} - \log \frac{e^{d_i^{\mathsf{T}} f_{y_i}^2 + b_{y_i}^2}}{\sum_{j=1}^{c} e^{d_i^{\mathsf{T}} f_j^2 + b_j^2}}$$

 $+\lambda_1\|F^1\|_2+\lambda_1\|F^2\|_2+\lambda_1\|b^1\|_2+\lambda_1\|b^2\|_2$ 

$$+\lambda_2 \sum_{j=1}^{c} \left| f_j^{1\top} f_j^2 \right|$$



### The multiverse network during test



### Surprising properties emerge

- I. The solutions are indeed orthogonal...
  ... but they all give the same softmax probabilities
- II. The dimensionality drops abruptly
- III. The Fisher Spectrum improves



### Cross entropy loss supports multiplicity

 Due to the properties of the softmax, there are multiple ways to get the same probabilities

**Lemma 1.** The minimizers  $F^*$ ,  $b^*$  of the cross entropy loss L are not unique, and it holds that for any vector  $v \in \mathbb{R}^c$  and scalar s, the solutions  $F^* + v \mathbb{1}_c^T$ ,  $b^* + s \mathbb{1}_c$ are also minimizers of L. *Proof*. denoting  $V = v \mathbb{1}_c^T$ ,  $s = s \mathbb{1}$ .

 $L(F^* + V, b^* + \boldsymbol{s}, D, \boldsymbol{y}) =$ 

$$\begin{split} &-\sum_{i=1}^{n} \log \left( \frac{e^{d_{i}^{T}f_{y_{i}}+d_{i}^{T}v+b_{y_{i}}+s}}{\sum_{j=1}^{c} e^{d_{i}^{T}f_{j}+d_{i}^{T}v+b_{j}+s}} \right) \\ &= -\sum_{i=1}^{n} \log \left( \frac{e^{d_{i}^{T}v+s}e^{d_{i}^{T}f_{y_{i}}+b_{y_{i}}}}{\sum_{j=1}^{c} e^{d_{i}^{T}v+s}e^{d_{i}^{T}f_{j}+b_{j}}} \right) \\ &= -\sum_{i=1}^{n} \log \left( \frac{e^{d_{i}^{T}v+s}e^{d_{i}^{T}f_{y_{i}}+b_{y_{i}}}}{e^{d_{i}^{T}v+s}\sum_{j=1}^{c} e^{d_{i}^{T}f_{j}+b_{j}}} \right) \\ &= -\sum_{i=1}^{n} \log \left( \frac{e^{d_{i}^{T}f_{y_{i}}+b_{y_{i}}}}{\sum_{j=1}^{c} e^{d_{i}^{T}f_{j}+b_{j}}} \right) = L(F^{*}, b^{*}, D, y) \end{split}$$

### If full rank, then Lemma 1 is IFF

 For full rank representation D the construction shown in Lemma 1 is the only way to obtain multiplicity

**Theorem 1.** Assume the minimal loss  $L^*(D, y)$  is obtained at two solutions  $F^1$ ,  $b^1$  and  $F^2$ ,  $b^2$ . If rank(D) = d, then there exists some vector  $v \in \mathbb{R}^c$  and some scalar s such that  $F^1 - F^2 = v \mathbb{1}_c^T$  and  $b^1 - b^2 = s \mathbb{1}_c$ .

Proof gist:

From the convexity of the cross entropy loss we infer a condition on the null space of the Hessian.

We show that for full rank representation, the Hessian has a zero singular value in only a few restrictive directions.

*Proof*. Let  $\Psi = [\psi_1, \psi_2, ..., \psi_c] = F^2 - F^1$ , and let  $\psi$  denote the concatenation of the column vectors  $\psi_{1...c}$  into a single column vector. From convexity:

$$\psi^T \nabla^2 L(D, y) \Big|_{F^1} \psi = \psi^T \frac{\partial L(D, y)^2}{\partial F \partial F} \Big|_{F^1} \psi = 0$$

For full rank D, we aim to prove that:  $\psi_1 = \psi_2 ... = \psi_c$ 

### Proof of theorem 1

The hessian can be written:

$$\begin{aligned} &\frac{\partial^2}{\partial F_{ju}F_{j'v}}L(D,y) = \\ &-\sum_{i=1}^n d_{iu}d_{iv}p_i(j)(\delta_{j=j'}(1-p_i(j)) - \delta_{j\neq j'}p_i(j')) \end{aligned}$$

After some manipulation:

$$\psi^{T} \frac{\partial^{2}}{\partial F \partial F} L(D, y) \Big|_{F^{1}} \psi = \sum_{j=1}^{c} \sum_{j'=j+1}^{c} (\psi_{j} - \psi_{j'})^{T} \sum_{i=1}^{n} d_{i} d_{i}^{T} p_{i}(j) p_{i}(j') (\psi_{j} - \psi_{j'})$$

$$\begin{split} &\sum_{i=1}^n d_i d_i^T p_i(j) p_i(j') \quad \text{-PD matrix} \\ &\sum_{j=1}^c \sum_{j'=j+1}^c \left( \psi_j - \psi_{j'} \right)^T \sum_{i=1}^n d_i d_i^T p_i(j) p_i(j') (\psi_j - \psi_j') \\ &\text{Vanishes if and only} \\ &\text{if } \psi_j = \psi_{j'} \end{split}$$

### ... now add orthogonality to the mix

 For full rank representations D multiple orthogonal classifiers are only possible for very specific (degenerate) classifier collections

**Theorem 2.** Assume that rank(D) = d, that d < c, and that the minimal loss  $L^*(D, y)$  is obtained at a solution  $F^1$ ,  $b^1$ . If there exists a second minimizer  $F^2$ ,  $b^2$  such that for all  $j \in [1 \dots c]$  the orthogonality constraint  $f_{j^1}^1 \perp f_{j^1}^2$  holds, then  $F^1$  admits to a stringent second order constraint.

Proof gist:

We employ theorem 1 and get equations of the form

$$F^{1T}v = -\begin{pmatrix} \left\|f_{1}^{1}\right\|^{2} \\ \left\|f_{2}^{1}\right\|^{2} \\ \vdots \\ \left\|f_{c}^{1}\right\|^{2} \end{pmatrix}$$

## The good news

- It is possible to obtain multiple orthogonal solutions that are almost as good as a single solution
- It requires the existence of small singular values in D
- Hence the low rank property

**Theorem 3.** There exist sets of weights  $F^1$ =  $[f_1^1, f_2^1, ..., f_c^1], b^1, F^2 = [f_1^2, f_2^2, ..., f_c^2], b^2$  which are orthogonal as follows  $\forall j \ f_j^1 \perp f_j^2$ , for which the joint loss:  $J(F^1, b^1, F^2, b^2, D, y) = L(F^1, b^1, D, y) + L(F^2, b^2, D, y)$ is bounded by  $2L^*(D, y) \leq J(F^1, b^1, F^2, b^2, D, y) \leq 2L^*(D, y) + A\lambda_d$ where A is a bounded parameter.

### The good news (enlarged)

**Theorem 3.** There exist sets of weights  $F^1 = [f_1^1, f_2^1, ..., f_c^1], b^1, F^2 = [f_1^2, f_2^2, ..., f_c^2], b^2$ which are orthogonal, i.e.,  $\forall j \ f_j^1 \perp f_j^2$ , for which the joint loss:  $J(F^1, b^1, F^2, b^2, D, y) = L(F^1, b^1, D, y) + L(F^2, b^2, D, y)$ is bounded by

 $2L^*(D, y) \leq J(F^1, b^1, F^2, b^2, D, y) \leq 2L^*(D, y) + A\lambda_d$ where A is a bounded parameter,  $\lambda_d$  is the smallest singular value of D.

### Proving Theorem 3

Proof gist: Using series expansion around  $F^1 = F^*$ 

 $L(F^{1} + \Psi, b^{1}) = L(F^{1} + \Psi, b^{1}) + (\vec{\nabla}^{T}\psi) L(D, y) \Big|_{F^{1}, b^{1}} + R(\psi)$ 

The remainder term (Lagrange form):

 $R(\psi) = \frac{1}{2} \left( \vec{\nabla}^T \psi \right)^2 L(D, y) \Big|_{\theta}$ =  $\frac{1}{2} \sum_{j=1}^c \sum_{j'=j+1}^c (\psi_j - \psi_j')^T \sum_{i=1}^n d_i d_i^T p_i(j) p_i(j') (\psi_j - \psi_j')$  $\leq \frac{1}{2} \sum_{j=1}^c \sum_{j'=j+1}^c (\psi_j - \psi_j')^T DD^T (\psi_j - \psi_j')$  **Theorem 3 generalization.** There exist sets of weights  $F^1 = [f_1^1, f_2^1, ..., f_c^1], b^1 ... F^m = [f_1^m, f_2^m, ..., f_c^m], b^m$  which are orthogonal as follows  $\forall ijk \ f_j^i \perp f_j^k$ , for which the joint loss:

$$J(F^{1}, b^{1} \dots F^{m}, b^{m}, D, y) = \sum_{r=1}^{m} L(F^{r}, b^{r}, D, y)$$
$$mL^{*}(D, y) \leq J(F^{1}, b^{1} \dots F^{m}, b^{m}, D, y)$$
$$\leq mL^{*}(D, y) + \sum_{l=1}^{m-1} A_{l} \lambda_{d-l+1}$$

### **Compact representation**

- Dim of representation turns out to be extremely compact
- No loss in energy
- Convergence to "natural" dim



### **Compact representation**

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- No loss in energy
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51 dimensional representation!

### Fisher Spectrum betterment

Between class covariance:

$$S_{b} = \frac{1}{n} \sum_{j=1}^{c} n_{j} (\mu - \mu_{j}) (\mu - \mu_{j})^{T}$$

Within class covariance:

$$S_{w} = \frac{1}{n} \sum_{j=1}^{c} \sum_{i \in I_{j}} (d_{i} - \mu_{j}) (d_{i} - \mu_{j})^{T}$$

Fisher spectrum:

$$S_b v = \gamma S_w v$$

Fisher ratio:

$$\sigma(v, S_b, S_w) = \frac{v^T S_b v}{v^T S_w v}$$



### How to measure post-transfer success

- The Joint Bayesian (JB) method is a popular learning face verification method Chen et al. Bayesian face revisited: a joint formulation. ECCV, 2012
- Two densities are learned

P(d, d'|H) and P(d, d'|I)

*H*: Same hypothesis*I*: Not same hypothesis



### Good Fisher Spectrum - Good JB separation

**Theorem 5.** Given data D, mean  $\mu$  and labels y, for any centered data point  $\hat{d}_i = d_i - \mu$ , we denote  $d'_i = (S_b + S_w)^{-1} \hat{d}_i$ . Given two centered data points  $\hat{d}_1, \hat{d}_2$  such that the fisher ratios  $\sigma(d'_1, S_b, S_w), \sigma(d'_2, S_b, S_w) < T$ , it holds that:



"Difficult to tell if same or not-same if all the difference between the faces is in directions with low fisher scores"



## The emergence of high fisher scores

- We prove the emergence of better fisher spectrum using S<sub>w</sub> orthogonality.
  - $$\begin{split} F^1 &= [f_1^1, f_2^1, \dots, f_c^1] \\ F^2 &= [f_1^2, f_2^2, \dots, f_c^2] \end{split} \quad \forall_j, f_j^1 \bot S_w f_j^2 \end{split}$$
- Experimentally, improved fisher spectrum is demonstrated in both types of orthogonality

**Theorem 6.** Let  $f^1 \dots f^m$  be a set of m classifiers that are  $S_w$ -orthogonal for data D and labels y, and let  $\gamma = [\gamma_1 \dots \gamma_d]$  denote the Fisher spectrum. Given that  $\forall 1 \leq r \leq m$ , for some value  $\theta$ ,  $\sigma(f^r, S_b, S_w) \geq \theta$ , it holds that  $\sum_{k=1}^d \gamma_k \geq \sqrt{m}\theta$ .



#### CIFAR-100 thumbnail recognition



#### LFW face recognition

#### Same



















### CIFAR-100 thumbnail recognition

- CIFAR-100
  - Learn on 90 classes
  - Transfer to the remaining 10







Architecture: NIN

Lin, Chen, Yan. Network in Network. ICLR, 2014

Layer	Filter/Stride	#Channel	#Filter
Conv11	5 imes5 / $1$	3	192
Conv12	$1 \times 1 / 1$	192	160
Conv13	$1 \times 1 / 1$	160	96
Pool1	3 imes 3 / $2$	96	-
Dropout1-0.5	_	_	-
Conv21	5 imes5 / $1$	96	192
Conv22	$1 \times 1 / 1$	192	192
Conv23	$1 \times 1 / 1$	192	100
Pool2	3 imes 3 / $2$	192	-
Dropout1-0.5	_	_	-
Conv31	3 imes 3 / $1$	192	192
Conv32	$1 \times 1 / 1$	192	192
Conv33	$1 \times 1 / 1$	192	100
Avg Pool	$7 \times 7 / 1$	100	-
FC	1 imes100 / $1$	100	100

### CIFAR-100 Results

Domain	Source	Target (transfer)	
Metric	Val error	Cosine	JB
M1	0.340	0.789	0.800
M2	0.340	0.791	0.804
M2 ( $S_w$ -orthogonal)	0.344	0.798	0.803
M3	0.345	0.801	0.812
M3 ( $S_w$ -orthogonal)	0.346	0.799	0.811
M4	0.351	0.807	0.82
M4 ( $S_w$ -orthogonal)	0.353	0.808	0.823
M5	0.360	0.812	0.833
M5 ( $S_w$ -orthogonal)	0.362	0.811	0.831
M6	0.369	0.816	0.838
M6 ( $S_w$ -orthogonal)	0.371	0.816	0.834
M7	0.375	0.815	0.831
M7 ( $S_w$ -orthogonal)	0.377	0.816	0.830





## LFW face recognition

- Learn on CASIA dataset
- Use the Scratch architecture from the CASIA paper
  - Yi, Lei, Liao, Li. Learning face representation from scratch. arXiv, 2014
- Transfer to LFW

#### The network used

Layer	Filter/Stride	#Channel	#Filter
Conv11	$3 \times 3 / 1$	1	32
Conv12	$3 \times 3 / 1$	32	64
Max Pool	2  imes 2 / $2$	64	_
Conv21	$3 \times 3  /  1$	64	64
Conv22	$3 \times 3 / 1$	64	128
Max Pool	2  imes 2 / $2$	128	_
Conv31	$3 \times 3 / 1$	128	96
Conv32	$3 \times 3 / 1$	96	192
Max Pool	$2 \times 2 / 2$	192	-
Conv41	$3 \times 3 / 1$	192	128
Conv42	$3 \times 3  /  1$	128	256
Max Pool	2  imes 2 / $2$	256	_
Conv51	$3 \times 3 / 1$	256	160
Conv52	$3 \times 3 / 1$	160	320
Avg Pool	$6 \times 6 / 1$	320	_
Dropout1-0.3	-	_	_
FC	$1 \times 320 / 1$	320	100

### LFW results

Domain	Source	Target (transfer)		
Metric	Val error	Cosine	JB on source	JB on LFW splits
CASIA trained M1	0.07	$0.962 \pm 0.0032$	$0.966 \pm 0.0022$	$0.970 \pm 0.0016$
CASIA trained M1 (2)	0.07	$0.962 \pm 0.0021$	$0.966 \pm 0.0019$	$0.971 \pm 0.0022$
CASIA trained M1 (3)	0.07	$0.961 \pm 0.0022$	$0.966 \pm 0.0013$	$0.971 \pm 0.0015$
Ensemble of 3 CASIA M1		$0.968 \pm 0.0019$	$0.972 \pm 0.0021$	$0.975 \pm 0.0025$
CASIA trained M2	0.08	$0.970 \pm 0.0021$	$0.974 \pm 0.0017$	$0.976 \pm 0.0016$
CASIA trained M3	0.11	$0.972 \pm 0.0012$	$0.977 \pm 0.0015$	$0.980 \pm 0.0034$
CASIA trained M3 (2)	0.11	$0.971 \pm 0.0031$	$0.977 \pm 0.0028$	$0.979 \pm 0.0027$
CASIA trained M5 (1)	0.12	$0.973 \pm 0.0011$	$0.978 \pm 0.0014$	$0.981 \pm 0.0019$
CASIA trained M5 (2)	0.12	$0.972 \pm 0.0015$	$0.977 \pm 0.0019$	$0.980 \pm 0.0031$
3rd party DB, M5	0.12	$0.982 \pm 0.0034$	$0.982 \pm 0.0031$	$0.988 \pm 0.0035$
Two network ensemble		$0.985 \pm 0.0029$	$0.990 \pm 0.0027$	$0.991 \pm 0.0027$

### Compared to SOTA

Method	Single network	Ensemble result	#nets	Training dataset	
M5	$0.9814 \pm 0.0019$	_		CASIA [41]	Excellent single
M5, 3rd party DB	$0.9883 \pm 0.0035$	0.9905 + 0.0027	2	proprietary 800k images	network result
DeepFace [32]	$0.9700 \pm 0.0087$	$0.9735 \pm 0.0025$	7	proprietary, 4M images	
DeepID [28]	_	$0.9745 \pm 0.0026$	25	proprietary,160k	Relativley small
Original scratch [41]	$0.9773 \pm 0.0031$	-	1	CASIA [41]	, dataset
Web-Scale Training [33]	0.9800	0.9843	4	proprietary, 500M images	
MSU TR [38]	$0.9745 \pm 0.0099$	$0.9823 \pm 0.0068$	7	CASIA [41]	Extrmely compact
MMDFR [5]	$0.9843 \pm 0.0020$	$0.9902 \pm 0.0019$	8	proprietary,500k	representation r1D
DeepID2 [25]	0.9633	$0.9915 \pm 0.0013$	25	proprietary,160k	
DeepID2+ [29]	0.9870	$0.9947 \pm 0.0012$	25	proprietary,290k	
FaceNet [23]	$0.9887 \pm 0.0015$	$0.9963 \pm 0.0009$	8	proprietary, 200M	
FR+FCN [43](*)	_	$0.9645 \pm 0.0025$	5	CelebFaces [27], 88k	
betaface.com(*)	_	$0.9808 \pm 0.0016$	NA	NA	
Uni-Ubi(*)	_	$0.9900 \pm 0.0032$	NA	NA	
Face++ [42](*)	-	$0.9950 \pm 0.0036$	4	proprietary, 5M face images	
DeepID3 [26](*)	-	$0.9953 \pm 0.0010$	25	proprietary,300k	
Tencent-BestImage(*)	_	$0.9965 \pm 0.0025$	20	proprietary, 1M face images	
Baidu [19](*)	-	$0.9977 \pm 0.0006$	10	proprietary, 1.2M face images	
AuthenMetric(*)	-	$0.9977 \pm 0.0009$	25	proprietary, 500k face images	



Solid blue M<sub>5</sub>, Dotted red M<sub>3</sub>, Dashed magenta M<sub>1</sub>

### Next step: multiple mv layers





#### Can we use a network instead of JB?



(a) Cosine angle

#### (b) Kernel Methods

#### (c) Siamese Network

Chopra, Hadsell, LeCun. Learning a similarity metric discriminatively, with application to face verification. CVPR, 2005.

#### **Deep Siamese Architecture**



#### **Deep Siamese Architecture**



Q5: Is binary classification loss the most appropriate loss for a Siamese Architecture? A: No. Gadot and Wolf. PatchBatch. *CVPR 2016*.

#### **Optical flow**

Given multiple image compute the motion field between them.



#### Architecture: from a patch to a representation

Layer	Filter/Stride	Output size
Input	_	$1 \times 51 \times 51$
Conv1	3 imes 3 / $1$	$32 \times 49 \times 49$
<b>Batch Normalization</b>	_	$32 \times 49 \times 49$
Max Pool	2  imes 2 / $2$	$32 \times 25 \times 25$
Conv2	3 imes 3 / $1$	$64 \times 23 \times 23$
<b>Batch Normalization</b>	_	$64 \times 23 \times 23$
Max Pool	2 imes 2 / $2$	$64 \times 12 \times 12$
Conv3	3 imes 3 / $1$	$128 \times 10 \times 10$
<b>Batch Normalization</b>	_	$128 \times 10 \times 10$
Max Pool	2 imes 2 / $2$	$128 \times 5 \times 5$
Conv4	3 imes 3 / $1$	256  imes 3  imes 3
<b>Batch Normalization</b>	_	256  imes 3  imes 3
Max Pool	2 imes 2 / $2$	$256 \times 2 \times 2$
Conv5	$2 \times 2  /  1$	$512 \times 1 \times 1$
<b>Batch Normalization</b>	-	$512 \times 1 \times 1$

Table 1. The network model for representing a grayscale  $51 \times 51$  input patch as 512D vector. The Batch Normalization is our finegrained variant. Leaky ReLU units [26] (with  $\alpha = 0.1$ ) are used as activation functions following the five batch normalization layers.



#### DRLIM type Loss

Hadsell, Chopra, LeCun. Dimensionality reduction by learning an invariant

mapping. CVPR 2006.

Orig DrLIM

$$(1-Y)\frac{1}{2}D_w^2 + (Y)\frac{1}{2}\{\max(0, m - D_w)\}^2$$

#### **DRLIM type Loss**

Hadsell, Chopra, LeCun. Dimensionality reduction by learning an invariant

#### mapping. CVPR 2006.

$$\begin{array}{c|c} \mbox{Orig DrLIM} & (\mbox{spring model}) & (1-Y)\frac{1}{2}D_w^2 + (Y)\frac{1}{2}\{\max(0,m-D_w)\}^2 \\ \\ \mbox{CENT-DrLIM} & (1-Y)D_w^2 + (Y)\{\max(0,m^2-D_w^2)\} \end{array}$$



#### **DRLIM type Loss**

Hadsell, Chopra, LeCun. Dimensionality reduction by learning an invariant

mapping. CVPR 2006.



$$(1-Y)\frac{1}{2}D_w^2 + (Y)\frac{1}{2}\{\max(0, m - D_w)\}^2$$
$$(1-Y)D_w^2 + (Y)\{\max(0, m^2 - D_w^2)\}$$

$$(1-Y)\lambda D_w^2 + (Y)\lambda \{\max(0, m^2 - D_w^2)\} + (1-\lambda)(\sigma_0 + \sigma_1)$$



#### Benchmarks - KITTI2012/KITTI2015

Raw Optical Flow on KITTI2012 validation set - <u>~8% err</u>

Method	Out-Noc	Running time	Method	Fl-all	Running time
PatchBatch-ACCRTE-PS71	5.29%	60.5s	PatchBatch-ACCURATE	21.69%	50.5s
PatchBatch-ACCURATE	5.44%	50.5s	DiscreteFlow [28]	22.38%	3min
PH-Flow [39]	5.76%	800s	CPM-Flow (anon.)	24.24%	2s
FlowFields [1]	5.77%	23s	EpicFlow [32]	27.10%	15s
CPM-Flow (anon.)	5.80%	2s	FilteringFlow (anon.)	28.50%	116s
NLTGV-SC [30]	5.93%	16s	DeepFlow [38]	29.18%	17s
PatchBatch-FAST	5.94%	25.5s	HS [35]	42.18%	2.6m
DDS-DF [37]	6.03%	1m	DB-TV-L1 [40]	47.97%	16s
TGV2ADCSIFT [5]	6.20%	12s	HAOF [6]	50.29%	16.2s
DiscreteFlow [28]	6.23%	3m	PolyExpand [14]	53.32%	1s

Table 4. Top 10 KITTI2012 Pure Optic Flow Algorithms as published on the submission date. Out-Noc is the percentage of pixels with euclidean error > 3 pixels out of the non-occluded pixels Table 5. Top 10 KITTI2015 Pure Optic Flow Algorithms as of the submission date. Fl-all is the percentage of pixels with euclidean error > 3 pixels. The FAST network was not trained on this benchmark by the submission time.

#### **Benchmarks - MPI-Sintel**

Method	EPE all, 'final' pass
FlowFields [1]	5.810
CPM-Flow (anon.)	5.960
DiscreteFlow [28]	6.077
EpicFlow [32]	6.285
Deep+R [13]	6.769
PatchBatch-CENT+SD	6.783
DeepFlow2 (anon.)	6.928
PatchBatch-SPRG	7.188
SparseFlowFused [36]	7.189
DeepFlow [38]	7.212
FlowNetS+ft+v [15]	7.218
NNF-Local [9]	7.249
PatchBatch-SPRG+SD	7.281
PatchBatch-CENT	7.323
SPM-BP [25]	7.325
AggregFlow [16]	7.329



Table 6. Top MPI-Sintel results as of the submission date. Each number represents the EPE (end-point-error), averaged over all the pixels in the comparison images, using the 'final' rendering pass of MPI-Sintel. Four ACCURATE variants are shown. The CENT-FIGURE+SD network is ranked 6th as of the paper's submission date. The FAST network was not trained on this benchmark by that date. The TF+OFM method [22] (EPE 6.727) is removed from this table since it is not a pure optical flow method.

# I'VE SPOKEN ENOUGH. ANY QUESTIONS?



# THANKYOU

