

## Conversion from horizontal to vertical representation

Find the membership functions (=vertical representations) of the following fuzzy sets of real numbers.

### Exercise 2.1

$$\mathcal{R}_A(\alpha) = \begin{cases} \mathbb{R} & \text{if } \alpha = 0, \\ \{7, 8, 9, 10, 12, 13, 14, 15, 17, 19\} & \text{if } 0 < \alpha \leq 0.3, \\ \{7, 8, 10, 13, 14, 17, 19\} & \text{if } 0.3 < \alpha \leq 0.7, \\ \{8, 10, 14, 17\} & \text{if } 0.7 < \alpha \leq 1. \end{cases}$$

### Exercise 2.2

$$\mathcal{R}_B(\alpha) = \begin{cases} \mathbb{R} & \text{if } \alpha = 0, \\ \{7, 8, 10, 12, 13, 14, 15, 17, 19\} & \text{if } 0 < \alpha \leq 0.3, \\ \{7, 8, 10, 14, 17, 19\} & \text{if } 0.3 < \alpha \leq 0.7, \\ \{8, 10, 13, 14, 17\} & \text{if } 0.7 < \alpha \leq 1. \end{cases}$$

### Exercise 2.3

$$\mathcal{R}_C(\alpha) = \begin{cases} \mathbb{R} & \text{if } \alpha = 0, \\ [\alpha, 1/\alpha] & \text{if } 0 < \alpha < 1, \\ \{1\} & \text{if } \alpha = 1. \end{cases}$$

### Exercise 2.4

$$\mathcal{R}_D(\alpha) = \begin{cases} \mathbb{R} & \text{if } \alpha = 0, \\ [\alpha - 1, 1/\alpha] & \text{if } 0 < \alpha < 1, \\ \{1\} & \text{if } \alpha = 1. \end{cases}$$