Exercise from properties of fuzzy implications and fuzzy equivalence relations.

Exercise 5.1 Find which implications presented explicitly in the lecture satisfy the exchange axiom (for the same implication in all instances)

$$\alpha \stackrel{\cdot}{\rightarrow} (\beta \stackrel{\cdot}{\rightarrow} \gamma) = \beta \stackrel{\cdot}{\rightarrow} (\alpha \stackrel{\cdot}{\rightarrow} \gamma). \tag{I5}$$

Exercise 5.2 Find all binary relations R on the set $\{A, B, C\}$, which satisfy R(A, B) = 0.6 and are

- 1. standard equivalencies,
- 2. product equivalencies,
- 3. Lukasiewicz equivalencies.