

Fuzzy negations, complements, and intersections

Exercise 3.1

Fuzzy sets A, B have the following vertical representations:

$$\mu_A(x) = \begin{cases} \frac{x-1}{2}, & x \in [1, 3], \\ 1, & x \in [3, 6], \\ 4 - \frac{x}{2}, & x \in [6, 8], \\ 0, & \text{otherwise,} \end{cases}$$
$$\mu_B(x) = \begin{cases} \frac{x-2}{3}, & x \in [2, 5], \\ 1, & x \in [5, 6], \\ \frac{8-x}{2}, & x \in [6, 8], \\ 0, & \text{otherwise.} \end{cases}$$

1. Find for which λ the formula

$$\neg_{\lambda} \alpha = 1 - \sqrt{1 - (1 - \alpha)^{\lambda}}$$

defines a fuzzy negation \neg_{λ} . Draw a graph.

2. Find a fuzzy disjunction dual to the product conjunction with respect to the negation from part 1.
3. Find the fuzzy complement of A with respect to the negation \neg_{λ} from part 1.
4. Find the standard, product, and Łukasiewicz intersections of A and B .