

- ◆  $N$  - number of data points
- ◆  $w$  - fraction of inliers
- ◆  $s$  - size of the sample

Prob. of selecting a sample with all inliers<sup>3</sup>:  $\approx w^s$

Prob. of **not** selecting a sample with all inliers:  $1 - w^s$

Prob. of **not** selecting a good sample  $K$  times:  $(1 - w^s)^K$

**Prob. of selecting uncontaminated sample in  $K$  trials at least once:**

$$P = 1 - (1 - w^s)^K$$

<sup>3</sup>Approximation valid for  $s \ll N$ , see the [lecture notes](#)

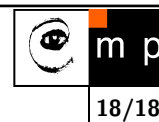
## Derivation of the probability

Drawing samples from a pool of data *without replacement* is not an independent process, it is not like tossing a coin. Assume  $N$  data points,  $I$  of them inliers. Probability of selecting one inlier in a random trial is clearly  $I/N$ . Probability of selecting another inlier from the remaining data set is  $(I - 1)/(N - 1)$ . The probability of selecting  $s$  uncontaminated (= all inliers) samples is then

$$P_s(I) = \prod_{i=0}^{s-1} \frac{I - i}{N - i}$$

which for small sample size and large number of points  $s \ll N$  may be well approximated as  $w^s$ .

**End**



## References