Fuzzy intersections

Exercise 4.1

Fuzzy sets A, B have the following horizontal representations:

$$\mathcal{R}_{A}(\alpha) = \begin{cases} \mathbb{R}, & \alpha = 0, \\ \left[1 + 2\alpha, 8 - 2\alpha\right], & \alpha \in (0, 1], \end{cases}$$
$$\mathcal{R}_{B}(\alpha) = \begin{cases} \mathbb{R}, & \alpha = 0, \\ \left[2 + 3\alpha, 8 - 2\alpha\right], & \alpha \in (0, 1]. \end{cases}$$

Find the standard, product, and Łukasiewicz intersections of A and B.